Abstract: In this opening introductory article to the issue of ZDM focused on mathematics education in Turkey, a short survey of the deep historical and cultural foundations of modern day Turkey is offered. This is followed by an outline of the development of researchers, as well as doctoral programs in mathematics education at universities in Turkey. The article also summarizes recently completed influential dissertations in Turkey and explains the aims and scope of this particular issue in relation to its conception and development.
Mathematics Education in Turkey- At the crossroads of cultural, political and economic currents

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Abstract

In this opening introductory article to the issue of ZDM focused on mathematics education in Turkey, a short survey of the deep historical and cultural foundations of modern day Turkey is offered. This is followed by an outline of the development of researchers, as well as doctoral programs in mathematics education at universities in Turkey. The article also summarizes recently completed influential dissertations in Turkey and explains the aims and scope of this particular issue in relation to its conception and development.

Keywords: curriculum development; doctoral programs in Turkey; history of Turkey; mathematics education research in Turkey;

Opening Remarks

I am pleased and honored to write this extended introduction to this special issue of ZDM focused on mathematics education in Turkey. This issue came about due to the convergence of a number of forces, namely three consecutive summer visiting professorships at Gazi University in Ankara, Turkey from 2007-2009 which led to exposure to the work of researchers, and the task of mentoring of doctoral students in mathematics education in Turkey. In the Fall of 2007 at Oberwolfach, I proposed the idea of doing a special issue of ZDM focused on Turkey, which was supported by both Gabriele Kaiser and Kristina Reiss, with the suggestion of using as much time as needed to produce a high quality issue. Three years later, it has come to be. We at ZDM are proud to claim that this is the very first issue of its kind in a mathematics education research journal that focuses on Turkey, continuing in the vein of the Brazilian issue. In this introductory article, my intention is to introduce the unfamiliar reader with the complex position that Turkey holds in the world due to its location, précis its unique historical and cultural development, familiarize the reader with the conceptualization, progress
and compilation of the issue, as well as convey the present state of the art of mathematics education in this unique country. Several myths abound in the West about Turkey, its culture and people due to Orientalism. Edward Said (1935-2003), the Palestinian American literary /critical theorist used this term to describe a tradition, both academic and artistic, of hostile and deprecatory views of the East by the West, shaped by the attitudes of the era of European imperialism in the 18th and 19th centuries (Said, 1979). When used in this sense, it often implies essentializing and prejudiced outsider interpretations of Eastern cultures and peoples.

A Brief History of Turkey [Introducing Ancient Turkey to Dummies]

The reader might be interested to learn that Turkish language and culture considerably influenced the languages and religions of Southern and Central Asia during the growth of the Moghul empire (Moghul is the Persian equivalent for Mongol). The Moghuls from the time of Tuglugh Timur (14th century), who had embraced Islam when the Mongol empire was splintering, were Turkic in origin and Persian in culture. Descendants of the Moghuls in the Indian sub-continent, such as Akbar the Great, and Shahjahan (the emperor who sanctioned the Taj Mahal) fused elements of Islam (particularly Sufism) with Hinduism. Although Turkish belongs to the western sub-group of the Oghuz language group, the language contains the strong influence of Farsi (Persian) and Arabic, and these languages in turn contribute to nearly 40% of the vocabulary of Hindi and Urdu. The uniqueness of Turkish culture is its historical relationship to the Greco-Roman and Byzantine worlds, the Caliphate and the Caucuses, making the land a true crossroads of civilizations (Sriraman, 2007, 2008).

Modern day Turkey established in 1923 following the fall of the Ottoman Empire in World War I is a secular democracy, western in its political and economic orientation as a result of the reforms initiated by Mustafa Kemal Pasha (1881-1938), also known as Atatürk2 (the father of modern Turkey). In modern Turkish the Arabic alphabet is eliminated and instead the Latin alphabet is used with linguistic symbols derived from French and German. I often posed the question-What does it mean to be Turkish? and interesting variations in responses arose. Many university intellectuals spoke of the various migrations, conquests and trans-migrations of Turkic tribes within Asia and to an extent in Europe, the battles for supremacy on the Anatolian lands in post-Genghis Khanates and agreed that the Osmanli (Ottoman) empire embraced, synthesized and nurtured numerous distinct cultures within its boundaries with an emphasis on fairness, respect and equality. In doing so the Turkish language evolved from its Oghuz-Uighur roots into one that bore a strong influence of Farsi (Persian), Hindustani and Arabic. On the other hand, some intellectuals and people who tended towards

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1 A serious introduction in the vein of the best selling Dummies series in academia and otherwise in the U.S
2 See Figure 1 for Atatürk’s transformation from soldier to statesman, diplomat and leader
modern Turkish nationalism emphasized more strongly the role and influence of
the Selguk (Ṣaljuqian in Farsi and Hindustani), in modern Turkish
identity. For the uninitiated, the Selguks’ origins lie in the Oghuz Turkic tribes (in
today’s geography, this is the region of Turkmenistan, Kazakhstan) that crossed
the Volga and settled into the Black Sea steppes and Khorasan around the 10th
century. Selguks became Persian in culture and language over time and then went
on to capture Turkey, and in a sense created a beautiful synthesis of Turkish and
Persian cultures. Another offshoot of this synthesis is found in India and Pakistan
in what is now known as the Moghul culture, a synthesis of Mongol-Turkic-
Persian cultures, one of the better consequences of the (infamous) Mongol
invasions starting with Genghis Khan. In a nutshell a documented history of
various Turkic nations stretches for 1500 years(!) from the 6th century onto 1921
[from small conglomerations of the Huns until the end of the Osmanli empire]. In
fact history textbooks in Turkey contain detailed maps of the migrations,
settlements and formation of Turkic nations over these 1500 years, and modern
day Turkey is the 16th nation!! When I queried about the reasons for frequent
invasions and battles for Anatolia- the answer was simple: The various kingdoms
lived in peace until some proclaimed themselves as the “Big Boss”. Such a
proclamation provoked neighboring Turkic kingdoms to attack. One should note
that the Selguks were a highly Persianized culture and originally not Islamic to
begin with. The Osmanli Empire at its peak spanned three continents [North
Africa, Eastern Europe, and Asia] and epitomized both modern day ideals of
justice, scientific research, tolerance, culture, equality as well as decadence. The
Osmanli alliance with the Germans in World War I contributed to their demise
and the formation of independent modern day Turkey was through bloody battles
fought on nearly all fronts of Turkey against the British, French and their allies.
The colors of the Turkish flag [Blood red with a white sliver moon and star]
symbolize the reflection of the moon and star on the bloodied soil (Sriraman,
2008).

Leaving these pleasantries aside, I will next introduce the two co-editors from
Turkey I invited to participate in compiling and putting together this issue.

Figure 1. Painting of Atatürk’s transformation from soldier to statesman to
founder of Modern Turkey
Background and research of Co-editors

Ziya Argün studied in two main research areas. His first main area of research is pure mathematics and his secondary area is mathematics education. In mathematics his research areas are topics in Functional Analysis and Operator Theories. His doctoral dissertation completed in at The University College of Wales in Aberystwyth was related to topics which are fundamental subjects in Functional Analysis and Operator Theories such as Banach Algebras, Arens semi-regularity of Banach algebras, Multipliers and quasi-multipliers on Banach algebras; finite rank, approximations, compact, nuclear and Integral operators on Banach spaces. He has successfully published some papers in these topics such as


After his dissertation he supervised two doctoral theses in Functional Analysis. In these theses his doctoral students researched topics like vector valued functions, vector measures, The Phillips Property, The weak Phillips Property, The Schur Property and Grothendieck Property which are part of geometric properties of Banach spaces and as a result they published some papers in these topics such as


2) Geometric properties of Banach spaces, Communications, Ankara University, Faculty of Sciences, 2005.


After the reconstruction of Education Faculties in Turkey in 1997, he like some mathematicians in the U.S and Germany started to research in the area of mathematics education. As a Full Professor at Gazi University, a state university with the largest teacher preparation program, he successfully initiated a PhD program in mathematics education, which has led to success. Under his supervision, several Ph. D. and many Master theses have been completed in research topics such as learning difficulties in algebra, teaching of algebraic concepts, cooperative learning, meta-cognitive behaviors, visual modeling as a component of pedagogical content knowledge, problem posing, problem solving strategies, the usage of visualization in abstractions and generalizations of mathematical concepts, students’ internal and external representations related to some mathematical concepts, concept images of prospective secondary mathematics teachers’, teaching of limit concept related to the functions of one and two variables. Some published articles related to mathematics education are:


The other co-editor Behiye Ubuz holds a BSc and MSc. from the Middle East Technical University (METU) at Ankara, and a Ph.D. from Nottingham University in United Kingdom. She specializes in mathematics education and is an associate professor at Middle East Technical University. Her research interests include various aspects of teaching and learning of mathematics, particularly calculus, geometry, fractions, decimals, and algebra. She has successfully published papers in numerous English language periodicals and in various international journals such as Journal of Computers in Mathematics and Science Teaching, The Journal of Mathematical Behavior, Academic Exchange Quarterly, and in Turkish language journals such as Egitim Fakültesi Dergisi, Egitim ve Bilim, İlköğretim online, Ondokuz Maviis Üniversitesi Egitim Fakültesi Dergisi, Pamukkale Üniversitesi Egitim Fakültesi Dergisi, Yaratici Drama Dergisi, Matematik Dünyası. Currently, she is working on proof and proving in algebra, geometry, etc; cognitive demands in tasks; pre-service teachers knowledge on functions and geometry etc. and supervising 6 PhD theses at METU.

In the next section I briefly summarize some innovative and influential that have come out of doctoral education programs in Turkey, particularly at Gazi University, which has spearheaded efforts at following qualitative methodologies in addition to setting a foundational base in the quantitative paradigm.

**Doctoral Dissertations**


The main aim of Dede’s study was to investigate the influence of teaching approach which is based on Keller’s (1987) ARCS motivation model and component display theory on students learning levels related to the concept of the variable and students’ motivation. The research was carried out in two phases, with quantitative and qualitative methods. In the qualitative part, the misunderstandings and the misconceptions of students’ related to the concept of the variable was investigated using a test which included 26 open ended

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3 The ARCS model was developed by John M. Keller. ARCS stands for Attention, Relevance, Confidence, and Satisfaction
questions. This test was administered to 8-grade students. In the quantitative part, the effect of the ARCS Motivation Model and Component display theory was investigated. To do this lessons were planed based on the ARCS Motivation Model and Component display theory and they were applied to the students of 8-grade.


The aim of Demircioglu’s study was to design educational events for the development of metacognitive behaviors (that is metacognitive knowledge and skills), to implement these educational events and to investigate the effects of these events on the behaviors of prospective mathematics teachers. In the designed educational events included different techniques like writing, thinking aloud, pair problem solving and action card. This study was organized in eight meetings (four of with writing, two with think aloud protocol, one of with paired problem solving and one with action cards) during the implementation of the whole processes. The data was collected through observations, written documents; think aloud protocol, videotapes, and audiotapes of semi structured interviews. The findings obtained indicated that having these carefully organized experimental studies improved the participants’ knowledge about themselves, increased their meta-cognitive behaviors, and increased their awareness. Also, after these experiments, participants began to work in critically self reflective ways, used control strategies and understood impediments to their success in the past.

The Transformation of Doctoral Dissertations from Turkish to English

It was a trend for mathematics education researchers such as many of the authors in this issue to receive their training abroad, either in the U.K or the U.S for their terminal degrees. Many of the authors in this issue received their PhD’s in the U.S and U.K. However with the systemic establishment of researchers within a core group of universities such as Gazi and METU, this trend has changed. Two recently completed dissertations at Gazi for which I served in an advisory capacity and an officially appointed committee member, the constructs of infinity and creativity were explored in great depth. What is special about these dissertations is that the PhD students conducted a part of the writing in English as opposed to only using Turkish.


Aztekin’s dissertation tackled the concept of infinity, first with a pilot study in young children through the use of animations and then compared it to the understanding of research level mathematics graduate students who had been exposed to formal set theory. His study yielded insights into the constructs about infinity held by PhD students as well as investigated the effects of the set theory
course on their informal models. This was achieved by using an innovative technique called repertory grid methodology as a way of capturing the constructs of students. A major component of the research on mathematics education related to infinity has been the study of student’s conceptions and reasoning about calculus subjects, particularly limits and series. Some related studies are about Cantor’s ordinal and cardinal infinity. However since most students at the high school and college level are unfamiliar with symbolic representations and terminology, such as a set theoretic approach, a context (generally geometric) is used for investigating notions of infinity indirectly. It was found that the PhD students in the study had an understanding of potential infinity and after the set theoretic lessons there was emerging evidence of the notion of actual infinity. One result was the tendency of interpreting different infinities which indicate element numbers of different infinite sets via countability and uncountability of sets. The other important result was about teaching of set theory topics. It was observed that students found ordinality harder than cardinality as studies at the past (Tirosh, 1991). Finally, Aztekin suggested repertory grid methodology (Fransella & Bannistiar, 1977) as a way of capturing the constructs of students and argued that this methodology can help us to learn further details about the understanding of infinity. This dissertation has resulted in the exploration and development of repertory grid methodology as a robust means of combining qualitative and quantitative paradigms for researching cognition in mathematics education (Aztekin, Arikan & Sriraman, 2010)


The main aim of this study was to extend the framework developed in Sriraman’s (2009, reprint of 2004) study on mathematical creativity and to determine the characteristics of creative thinking skills developed by secondary mathematics prospective teachers’ during the process of mathematical problem-solving. The study was motivated by the fact that although research mathematical activities are nested within creativity, the schools provide insufficient experiences related to creativity in mathematics. The main aim of the dissertation study was to determine pre-service secondary mathematics teachers’ creative thinking skills when presented with different mathematical problem-solving situations. Creative thinking was operationalized in terms of fluency, flexibility and originality, and examined using qualitative research methodology. Twenty two pre-service secondary mathematics teachers participated in this study during their optional course called ‘Selected Topics in Mathematics’. In order to obtain in-depth knowledge, and triangulation criteria, data included classroom observations, pre-service teachers’ journals, and semi-structured interviews. Coding techniques from grounded theory were used in the data analysis. The results of this study pointed out a number of issues related to mathematical creativity. It was found that pre-service teachers developed various problem-solving behaviors in different mathematical problem situations but also encountered various difficulties due to the types of algorithmic strategies used and the dead ends that some of these strategies led to. The research findings also pointed out that creative thinking skills in terms of fluency, flexibility and originality mainly depended on personal and extra cognitive factors.
Developing the Issue – The need for quality and coherence

As stated earlier, this special issue of ZDM was conceived as a result of my visiting appointments at Gazi University in Turkey over the course of three summers, during which time I served as a member of different theses’ Committees and as an academic collaborator. Having reported on some of the outcomes in the previous sections of this introduction, I now turn to the focus of this issue per se. The goal of this issue was to share some prototypical examples of research conducted in Turkey in mathematics education. For this reason, the issue editors planned an issue that originally cohered around the themes of cognition and curriculum, areas which have been researched extensively in Turkey. The papers solicited for this issue were meant to convey the state of research in the following areas in Turkey.

- History of Mathematics Education in Turkey in the context of K-12 mathematics curricula
- The story of change in the nationally unified curricula of Turkey and the quality of mathematical tasks in this new Turkish school mathematics curricula
- The structure of meta-cognitive behaviors displayed in the process of problem solving of prospective mathematics teachers in Turkey?

The opening article *A Brief History of Mathematics Education in Turkey: K-12 Mathematics Curricula*, gives a brief history of mathematics education in Turkey. The purpose is not to detail the whole history of Turkish Education but to give a snapshot of the history of Turkish Mathematics Education in the last century. In this context, the authors (Argün, Arikan, Bulut & Sriraman) underline some important events and eras that has affected the national education movements in Turkey from the curriculum development perspective since one of the main goals in this issue of ZDM is to share some prototypical examples of research conducted in Turkey in mathematics education. This article provides the reader with a general perspective for the historical development of K-12 mathematics curricula with respect to their philosophies, goals, objectives, instruction and assessment as opposed to a comprehensive analysis of the mathematics education in Turkey, so that the ensuing articles included in this issue can be understood more deeply and clearly. The second article “A micro-curricular analysis of unified mathematics curricula in Turkey” gives a brief description of the educational system in Turkey and is explicated on the main tenets of unified curriculum, especially in the area of mathematics. In this article, Zembat conducts an analysis of a newly developed mathematics curriculum that has been under revision for the last five years and being implemented for the last three years. The article includes an analysis of a sample lesson from a newly developed textbook written by the scholars working for Ministry of Education as well as approved by the Ministry. In a sense, Zembat tries to give the reader a sense for the issues about the (lack of) connection among the intended curriculum, written curriculum and implemented curriculum for the area of mathematics using the case of Turkey.
Two examples of research using phenomenological/hermeneutic methods are found in this issue, namely Inan & Dogan-Temur’s “Understanding Kindergarten Teachers’ Perspectives of Teaching Basic Geometric Shapes: a Phenomonographic Research” and Taşar’s article entitled “What Part of the Concept of Acceleration is Difficult to Understand: The Mathematics, the Physics, or both? Both articles focus on specific content related issues. The former is aimed at Turkish kindergarten classes and examines teachers’ perspectives on teaching geometry in kindergarten classes using phenomenographic methods. The findings of this phenomenographic research indicated lack of deep content knowledge, a finding similar to those in other parts of the world in the sub-domain of the teaching of geometry. The latter piece focuses on an individual learner and attempts to understand why and how learning is progresses in a particular direction and results in failure or success. Without posing a hypothesis, a freshman novice college student’s lines of thought and reasoning regarding force and motion in particular situations are investigated in order to portray an example of such learning. From a mathematics teaching point of view, Taşar considered velocity and acceleration as primary examples for students to truly comprehend the meaning of the concept of rate of change. The author reports that both velocity and acceleration are rate of change type concepts but while students can learn the former relatively easily, as demonstrated here, the latter causes a lot of conceptual difficulties. This study was the doctoral thesis of Taşar conducted in the U.S., and is included in the issue as an example of Turkish doctoral student’s exposure to qualitative methods outside their country.

The fifth article by Ubuz et al., entitled Exploring the quality of the mathematical tasks in the new Turkish elementary school mathematics curriculum guidebook: the case of algebra, is a prototypical example of a content related curriculum analysis in relation to the place of Algebra in the elementary school curriculum.

Finally the last article entitled by “A Case Study: Assessment of Preservice Secondary Mathematics Teachers’ Metacognitive Behaviors in Problem Solving Process” focuses on how pre-service secondary mathematics teachers’ meta-cognitive behaviors change in solving different types of mathematical problems. The authors Demircioğlu, Argün & Bulut tried to answer the following questions:

1) How do the pre-service secondary mathematics teachers’ meta-cognitive behaviors change in solving mathematical problems when accounting for all possibilities strategies with respect to achievement?

2) How do the pre-service secondary mathematics teachers’ meta-cognitive behaviors change in solving mathematical problems when making a drawing, and intelligent guessing-testing strategies with respect to achievement?

In order to investigate these problems an exploratory case study methodology was used with 45 mathematics pre-service teachers. Existing problem solving frameworks were operationalized to research and analyze participants’ think aloud protocols. As a consequence of the analysis it was found that there was no relationship between academic achievement and frequencies of meta-cognitive behaviors.

The papers submitted for the issue were subject to rigorous review, which resulted in acceptance (and improvement) of many and rejection of others. The selection
process began with the submission of 15 abstracts, from which 12 were invited to submit full papers. After two rounds of peer review including numerous rewrites and revisions, six papers were accepted, which significantly advances our understanding what characterizes mathematics education research in Turkey today. The value of the set of papers lies in their exploration of history, curriculum and cognition. Some of the papers in this issue cover research and history of curriculum, whereas the others focus on specific implementation issues of content such as geometry and algebra in the curriculum.

**Concluding Notes**

Mathematics education in Turkey is following the natural progression of development as witnessed in numerous countries such as the U.S., Australia, U.K and Germany. The field originated in the work of mathematicians who turned into pedagogues, with ensuing generations becoming more trained and proficient with terminal degrees in mathematics education from the U.S, U.K, and Turkey itself. Researchers in Turkey are also gradually moving from topics researched in other parts of the world such as affect, meta-cognition and problem solving, gender issues using quantitative methodologies onto more qualitatively oriented methods such as repertory grid methodology (Aztekin, Arikan, Sriraman, 2010), grounded theory, and phenomenological methods to explore more complex and nuanced phenomenon such as creativity. Research on curriculum has also been traditionally robust and continues in addition to large scale studies on gender issues (e.g., Bulut, Gur, Sriraman, 2010). Turkey is a very “young” country in terms of its demographics with many talented and energetic students in mathematics education and other fields. I anticipate many of them making good contributions to scholarship and curriculum development. On a larger scale, the infrastructure and economy of the country is booming and there is a vibrant energy about it. However, it still remains unclear whether the EU will judge Turkey for its secular, economic, political and institutional merits and offer it membership or whether the collective consciousness of the EU is still haunted by the Osmanli flag flying across the Danube during the last siege of Vienna in 1683 (Sriraman, 2008). Only time will tell!

**References**


**Reviewers for the Issue**

I wish to acknowledge and thank numerous mathematics educators in Turkey and in other parts of the world that played a pivotal behind the scenes role in improving the manuscripts, besides the hundreds of hours spent by the author to provide writing support, compile, edit and language corrections needed for this issue. The 30 reviewers who played a role through many rounds of reviews to help authors improve their papers will be acknowledged at the end of the year. The efforts of several Turkish colleagues to conduct English language corrections for various authors in the issue is also much appreciated. Several international reviewers reported to me the learning experience of understanding the depth, the history and the complexities of mathematics education in Turkey.

**Acknowledgements**

The author thanks Gazi University, their mathematics education faculty and doctoral students at the Institute of Educational Sciences for their hospitality during my visits. In particular I am grateful to Ziya & Gulfer Argun, Ahmet & Aynur Arıkan, Yasemin & Onur Kıymaz for immersing me into Turkish language, culture and making me a part of their families. In addition Rezzan Yılmaz, Hakan Sandir and numerous others that I have forgotten to name here have been extremely generous with their time and grace during my visits.